Please check the examination details bel	ow before ente	ring your candidate information
Candidate surname		Other names
Centre Number Candidate No		
Time 2 hours	Paper reference	AAL30/01
Algebra Level 3 Calculator NOT allowed		• •
You must have: Ruler graduated in centimetres and n pair of compasses, pen, HB pencil, era		Total Marks

Instructions

- Use **black** ink or ball-point pen.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Answer the questions in the spaces provided - there may be more space than you need.
- Calculators are not allowed.

Information

- The total mark for this paper is 90
- The marks for **each** question are shown in brackets
 - use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ▶





Answer ALL questions.

Write your answers in the spaces provided.

You must write down all the stages in your working.

You must NOT use a calculator.

1 (a) Expand and simplify
$$(y+3)(2y-3)$$

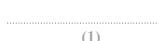
(b) Expand and simplify $(2 + 5x)^2$



(c) Simplify $(8r^{12})^{\frac{1}{3}}$



(d) Simplify $t^{-2} \times t^{-\frac{3}{4}}$



(Total for Question 1 is 7 marks)



2 Make x the subject of $w = \frac{3x^2 + 2}{x^2 + 1}$

(Total for Question 2 is 3 marks)

3 Use the quadratic formula to solve the equation $3x^2 - 2x = 6$ Give your answer in the form $\frac{p \pm \sqrt{q}}{r}$ where p, q and r are integers.

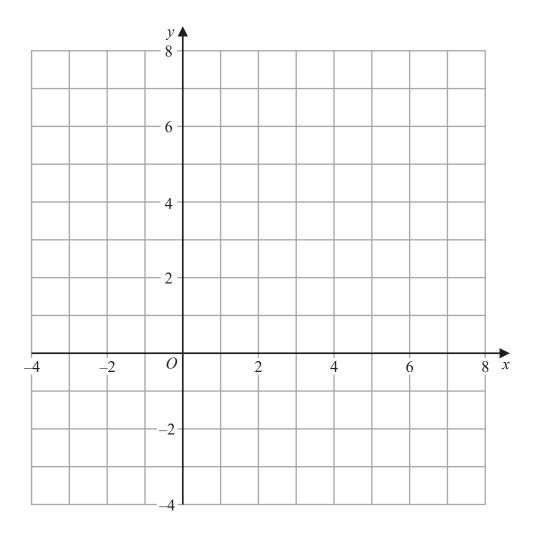
(Total for Question 3 is 2 marks)



4 On the grid, shade the region that satisfies all these inequalities.

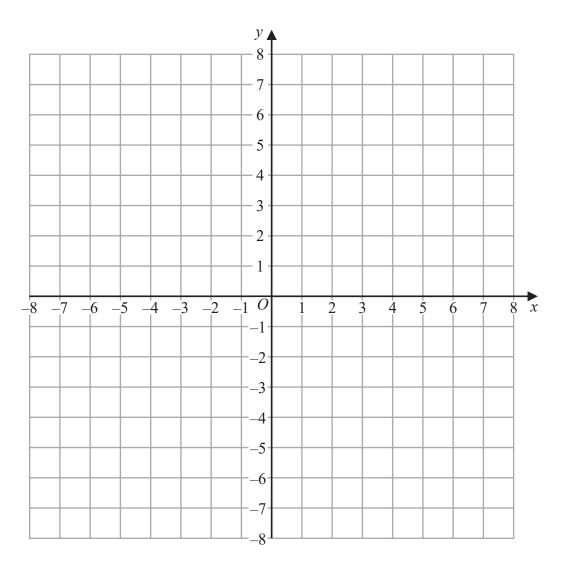
$$x > -2$$
 $y > 1$ $2x + 3y < 6$ $y < x + 4$

Label the region R.



(Total for Question 4 is 5 marks)

5 (a) On the grid, construct the graph of $x^2 + y^2 = 49$



(2)

Given that a > 0, the point A with coordinates (0, a) lies on the graph of $x^2 + y^2 = 49$

(b) Draw a tangent to this graph at A.

(1)

(Total for Question 5 is 3 marks)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

 $x^2 + x - 6$ (b) (i) Factorise

(1)

(ii) Hence solve $x^2 + x - 6 < 0$

(Total for Question 6 is 5 marks)

7 (a) Find an equation of the straight line which passes through the origin and is parallel to the straight line with equation 3x = 4y + 7

(1)

(b) Find the gradient of a line perpendicular to the line with equation 2x = 5y + 8

(2)

(Total for Question 7 is 3 marks)

8 Here is a quadratic equation.

$$9x^2 - 12x + 4 = 0$$

Use the discriminant to determine whether the equation has

2 real and different roots

or 2 real and equal roots

or no real roots.

(Total for Question 8 is 2 marks)



(b) Factorise $p^4 - p^2q^2$

(2)

(Total for Question 9 is 4 marks)

- **10** $x^2 + 6x + 13$ can be written in the form $(x + a)^2 + b$
 - (a) Find the value of a and the value of b.

(2)

The curve with equation $y = x^2 + 6x + 13$ has a turning point at the point A.

(b) Write down the coordinates of A.

(Total for Question 10 is 3 marks)

DO NOT WRITE IN THIS AREA

- 11 The first term of an arithmetic series is 4 The common difference of the series is 7
 - (a) Find an expression, in terms of n, for the nth term of the series. Give your answer in its simplest form.

(2)

(1)

The *p*th term of the series is 102

(b) Work out the value of p.

(c) Find the sum of the first 100 terms of this series.

(2)

(Total for Question 11 is 5 marks)



12 The average speed, v km/h, for a journey of a given distance is inversely proportional to the time, t hours, taken to complete the journey.

When v = 60, t = 4

(a) Find a formula for v in terms of t.

(3)

(b) Calculate the value of t when v = 80

(2)

(c) Using the axes below, sketch the graph of v against t.



(1)

(Total for Question 12 is 6 marks)

13 Here is a quadratic equation.

$$6x^2 + 5x - 12 = 0$$

(i) Write down the sum of the roots of this equation.

(1)

(ii) Write down the product of the roots of this equation.

(1)

(Total for Question 13 is 2 marks)

14
$$V = \frac{f(wh-3)}{3} + f$$

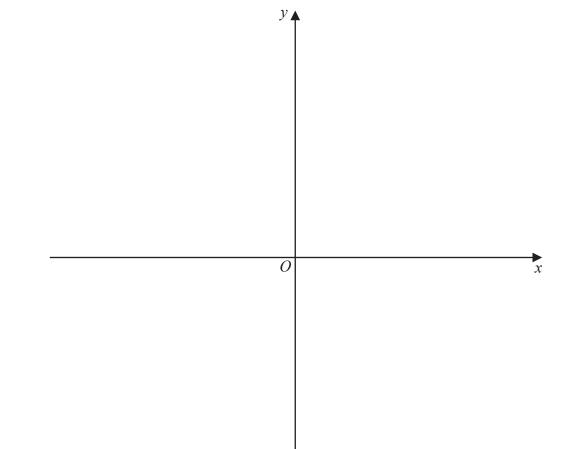
Work out the value of h when V = 20, f = 12 and $w = \frac{f}{2}$

(Total for Question 14 is 3 marks)



15 Using the axes below, sketch the graph $y = \frac{1}{x-2}$

Show clearly any asymptotes and the coordinates of any point of intersection of the graph with the axes.



(Total for Question 15 is 4 marks)

16 Solve the simultaneous equations

$$y = 3x^2 + 6x - 1$$
$$y - 1 = x$$

(Total for Question 16 is 4 marks)



17 (a) Expand and simplify $(3 + \sqrt{12})(5 - 3\sqrt{3})$

(3)

(b) Rationalise the denominator of
$$\frac{2 - \sqrt{13}}{1 - \sqrt{13}}$$

Give your answer in the form $\frac{p-\sqrt{13}}{q}$ where p and q are integers.

(3)

(Total for Question 17 is 6 marks)

18 The straight line L passes through the points A and B.

The coordinates of A are (3, -8)

The coordinates of B are (-1, 7)

Find an equation for L

Give your answer in the form ax + by + c = 0 where a, b and c are integers.

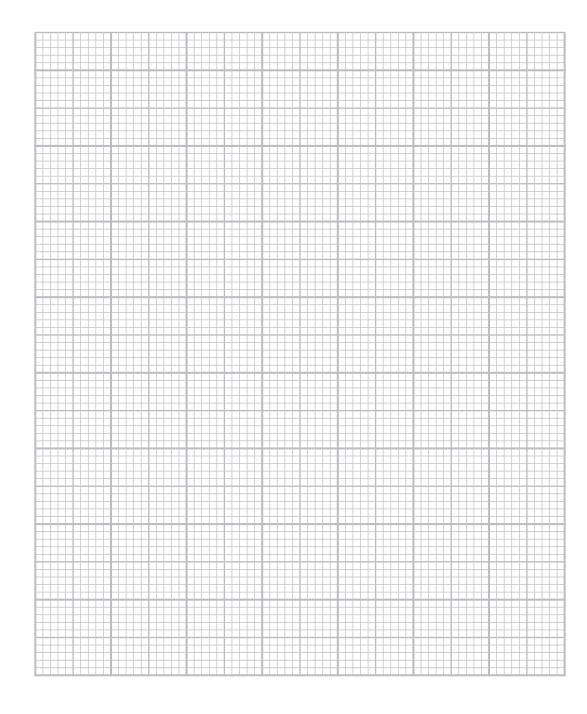
(Total for Question 18 is 3 marks)



19 The table shows the values of $y = 2^{x-1}$ for integer values of x from -2 to 4

x	-2	-1	0	1	2	3	4
у	$\frac{1}{8}$	$\frac{1}{4}$	$\frac{1}{2}$	1	2	4	8

(a) On the grid, draw the graph of $y = 2^{x-1}$ for values of x from -2 to 4



(2)



(b) Use your graph to find an estimate, to one decimal place, for the solution of $2^x = 12$

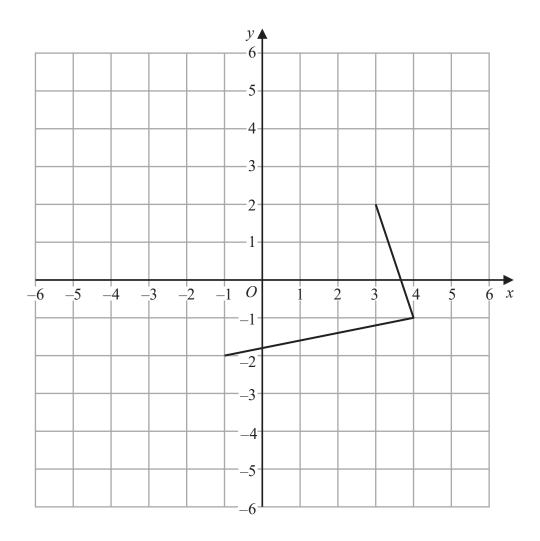
(2)

(c) Use the trapezium rule to find an estimate for the area of the region under the curve and between x = 1, x = 4 and the x-axis. Use 3 strips of equal width.

(2)

(Total for Question 19 is 6 marks)

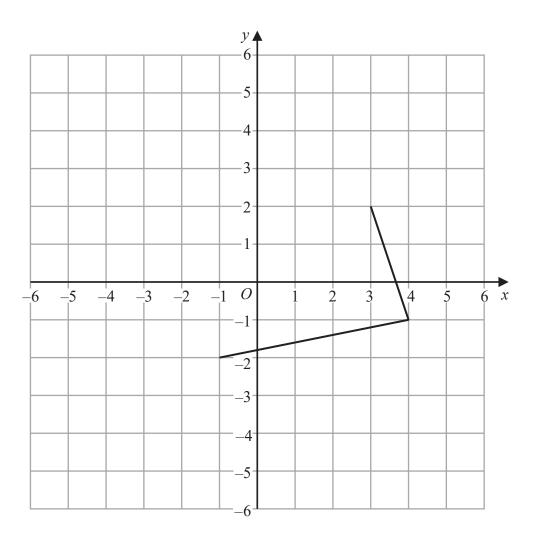
20 Here is the graph of y = f(x)



(a) On the grid above, draw the graph of y = f(x) - 2

(2)

Here is the graph of y = f(x)



(b) On the grid above, draw the graph of y = f(2x)

(2)

(Total for Question 20 is 4 marks)

21 (a) Express $\frac{3}{x+4} + \frac{1}{x-4}$ as a single fraction.

Give your answer in its simplest form.

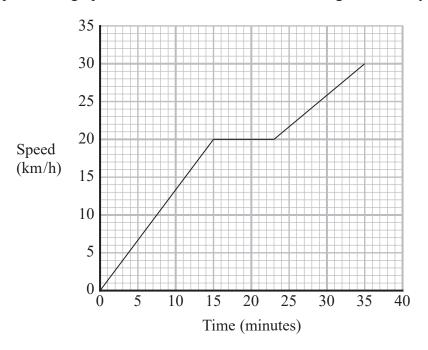
(b) Hence, or otherwise, solve $\frac{3}{x+4} + \frac{1}{x-4} = \frac{4}{5}$

(3)

(3

(Total for Question 21 is 6 marks)

22 Here is a speed-time graph for the first 35 minutes of a training ride for a cyclist.



(a) For how many minutes is the cyclist accelerating?

_____ minutes (1)

(b) Work out the greatest acceleration of the cyclist. Give your answer in km/h²

..... km/h²

(c) What does the area under the graph represent?

(1)

(Total for Question 22 is 4 marks)

TOTAL FOR PAPER IS 90 MARKS



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